

Sheer line formulation used in « Gene Hull Sailboat 3.5 » - 04 2026

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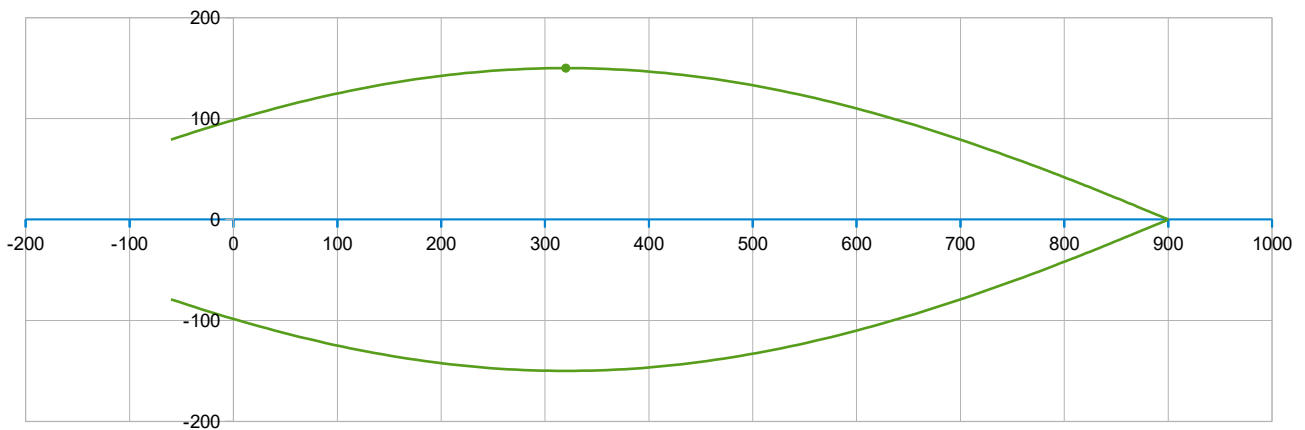
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Introduction :

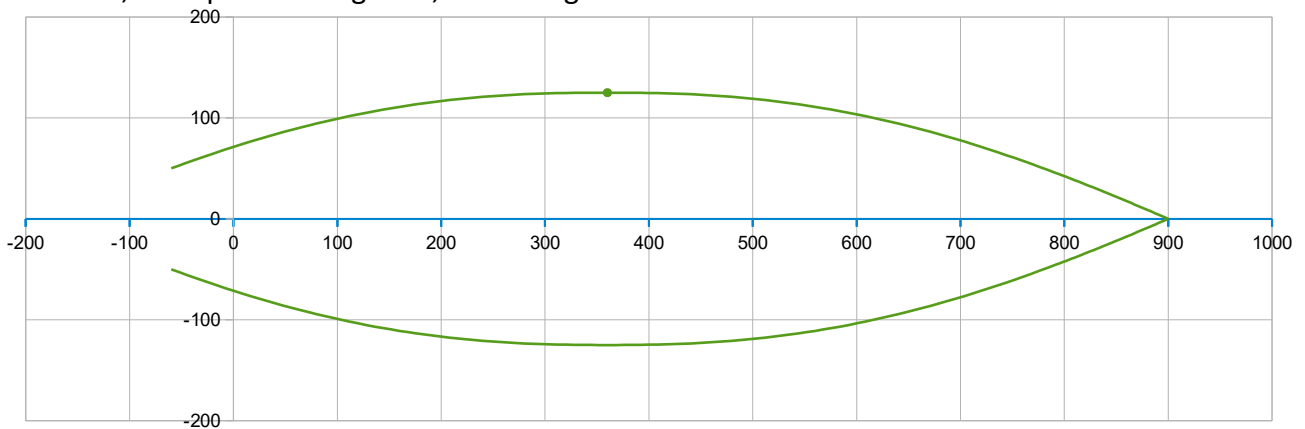
I think it might be interesting to introduce these formulations through my own approach from the beginning of Gene-Hull, to better highlight the reason of each step of complication.

At first, I wanted a very simple formulation, so I adopted a parabolic curve, that is to say a polynomial of degree 2. But it appears that the line towards the bow (and towards the stern to a lesser extent) was not taut enough compared to the usual designs, so I added a small complication : the degree 2 of the polynomial is slightly decreased as one approaches the forward and aft ends. It is the so-called « generic » sheer line here after.

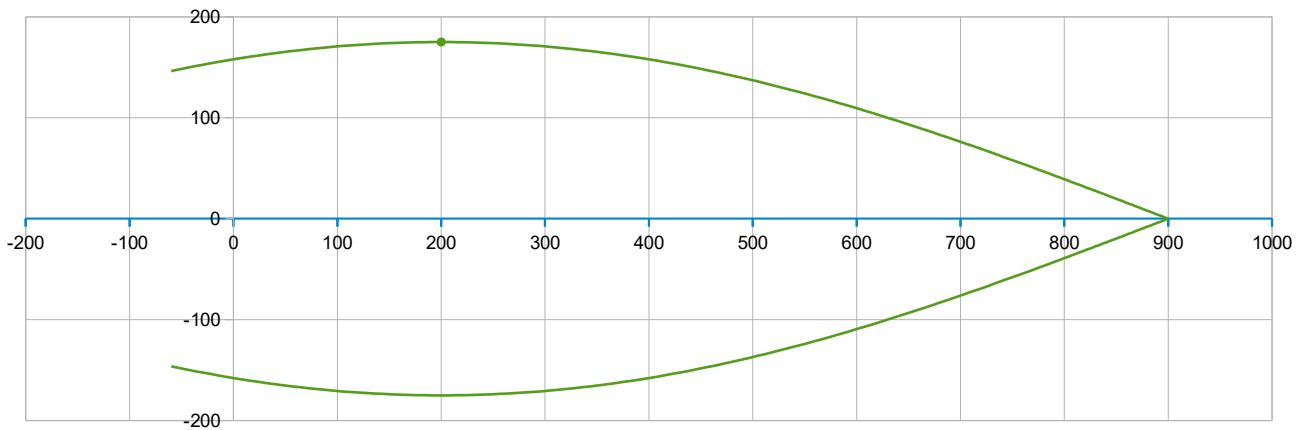
This generic sheer line works quite well for classic keel boat and IOR ones of the 60-70 years, the max beam and the max curvature of the sheer line are at the same X location, example (the point shows the maximum beam & curvature) :



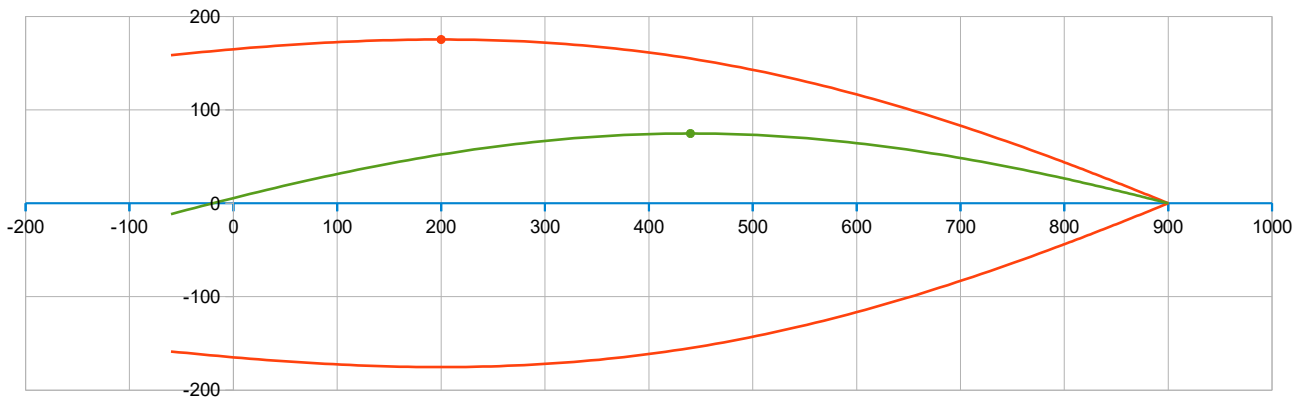
With a degree > 2 , the generic formulation can also generate the sheer line of some traditional sailboats, example with degree 2,4 showing a local flatness around the max beam location :



But the « generic » sheer line has its limit, and this became obvious when I wanted to represent the sheer line of a modern beamy sailboat as inspired by the Imoca class development since the 1990s. If I just increase the beam and put it backward, the sheer line looks not relevant when compared with the usual designs. Example :

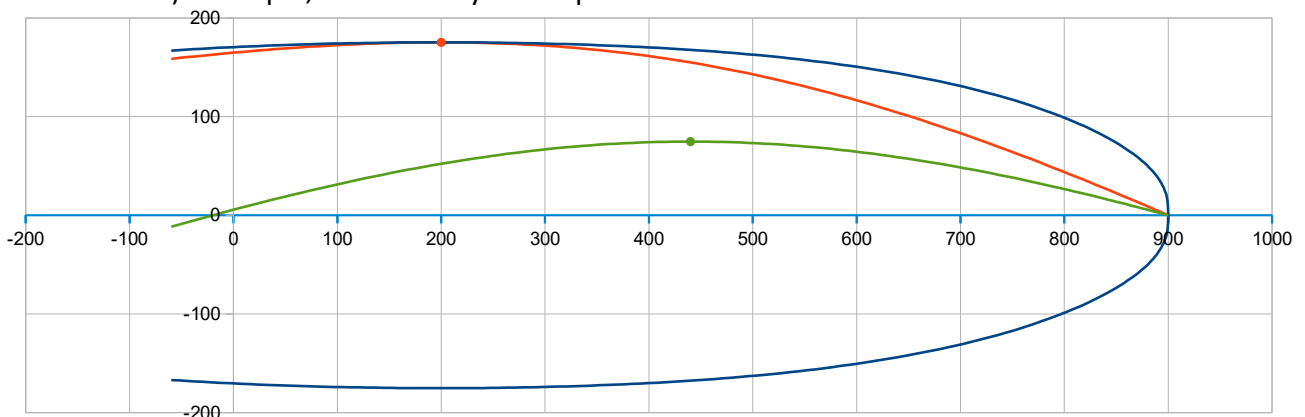


What is not good here above is the maximum curvature kept at the maximum beam, so very far aft. To remedy this, I had the idea of opening the lines like opening scissors, using the front point as the center of rotation, hence the so-called "Alfa" transformation (the angle of rotation). Example, a virtual « generic shear » line is drawn and then opened with the « Alfa » transformation in order to have the same max beam at the same location as above :



>>> the maximum beam is at X 200 as for the previous example but here the maximum curvature remains at ~ 440 where was the maximum beam of the virtual shear line. So the « Alfa » sheer line allows a greater variety of shapes for the sheer line, while with putting Alfa = 0 you still can return to the generic one.

But another family of shapes was still not possible, the scow type. So, I developed a third level of the formulation, so-called the « Alfa + Scow » sheer line, starting from the previous one (with Alfa active or not). Example, in continuity of the previous one :



>>> The Scow transformation keep unchanged the max beam and its location.

The shear line, in its horizontal projection xy

Coordinates system and notation :

x = 0 at section C0 (= rear point of the waterline), x positive towards front

y = 0 in the symmetrical longitudinal plan,

Ysheer(X) is renamed Y1(X) to simplify the formulations, as also done for the sections ones.

1) The generic shear line

This first shear line does not use the parameters Alfa and Scow (Alfa =0 ; Scow = 0) :

$$Y1(X) = Bg/2 - C * ABS(X - XBg)^{[Puilivy - Corpuiliv * (ABS(X - XBg)/(Xbow - XBg))^{Puicorpuil}]}$$

, where $C = (Bg/2) / (Xbow - XBg) ^{(Puilivy - Corpuiliv)}$
 $XBg = XBg (\% Lwl) * Lwl / 100$

Valid for X = Xlivar to Xbow ; ABS is the function « Absolute value of ... »

Data used for this formulation are :

Geometrical : Bg, Lwl, Xbow, XBg (%Lwl) (+ Xlivar for the range of X for the computation)

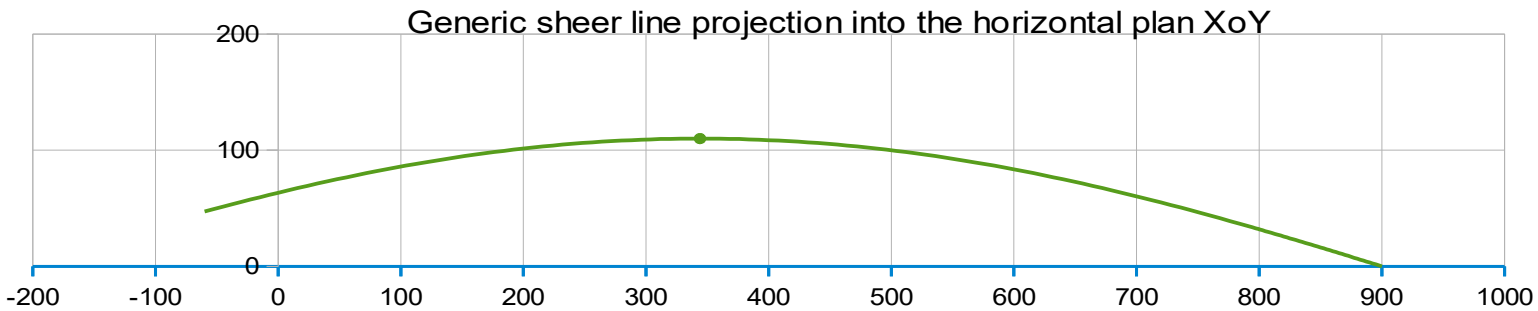
Adimensional parameter : Puilivy, Corpuilivy, Puicorpuil

Example with (from Boat V1) :

Lwl	800,0
Xbow	900,0
Xlivar	-60,0

Bg	219,9
XBg (% Lwl)	43,0

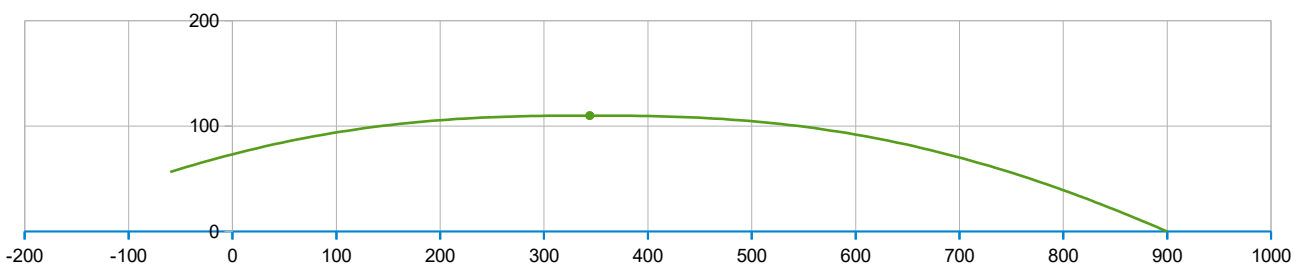
Puilivy	2,00
Corpuilivy	0,025
Puicorpuil	2,00



The green point is to show the location of the max Beam.

Puilivy = 2 is strongly recommended to have a smooth regularity of the curvature evolution, but you can also adopt Puilivy >2 to have some shear line that we can see for traditionnal sailboat.

Another example with Puilivy = 2,5, here you have a small flatness around the max beam position. In such case, you have no need to use the Alfa transformation described here after.



2) The sheer line transformed by Alfa

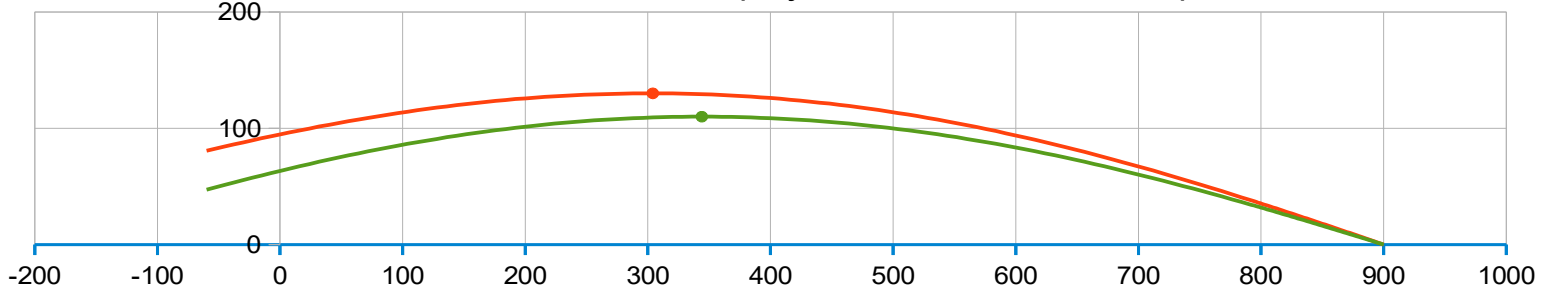
$$Y1 \text{ Alfa}(X) = -(X-X_{\text{bow}}) * \sin(\text{Alfa}) + Y1(X) * \cos(\text{Alfa})$$

for $X = X_{\text{livar}}$ to X_{bow}

The complementary data used is only Alfa (°)

Example with Alfa (°) = 2 , other above data being unchanged (from Boat V1) :

In red : sheer line with Alfa = 2°, projection into the horizontal plan XoY

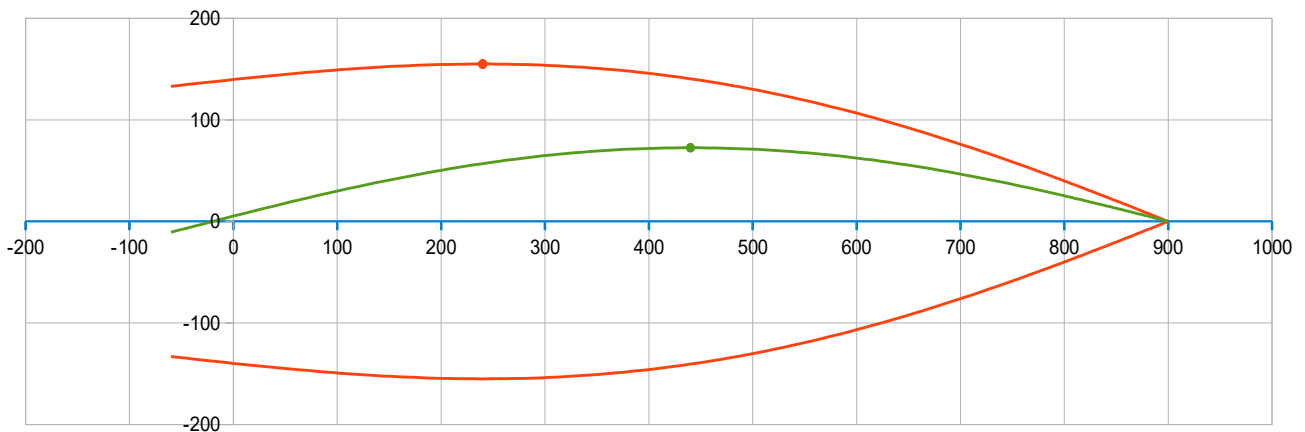


The red point shows the new location of the max Beam, of which value et position are output :

```
>>> Output data (cm)
      Bmax      260,0      at Xb(%Lwl)      38,0
```

Another example with :

Bg	145,1
X Bg (% Lwl)	55,0
Alfa (°)	8,60



```
>>> Output data (cm)
      Bmax      310,0      at Xb(%Lwl)      30,0
```

3) The shear line transformed by Alfa and Scow

$$Y1 \text{ Alfa} + \text{Scow}(X) = Y1 \text{ Alfa}(X) + \text{Scow}(X) * [B_{\text{max}}/2 - Y1 \text{ Alfa}(X)] * [(X_{\text{bow}} - X)/(X_{\text{bow}} - X_{B_{\text{max}}})]^{\text{Pui Scow}}$$

where :

$$\text{Scow}(X) = \text{Scow} * [1 - 0,5 * ((X_{\text{bow}} - X)/(X_{\text{bow}} - X_{\text{tabar}}))^2]$$

B_{max} is the maximum beam issued from $Y1 \text{ Alfa}(X)$ formulation

$X_{B_{\text{max}}}$ is the X location of B_{max}

(No formulation for these two last data, you should recover them by exploiting the $Y1 \text{ Alfa}(X)$ formulation , as done in the .ods file joined for test, cells P167 and Q169)

The complementary data used are :

Geometrical : X_{tabar}

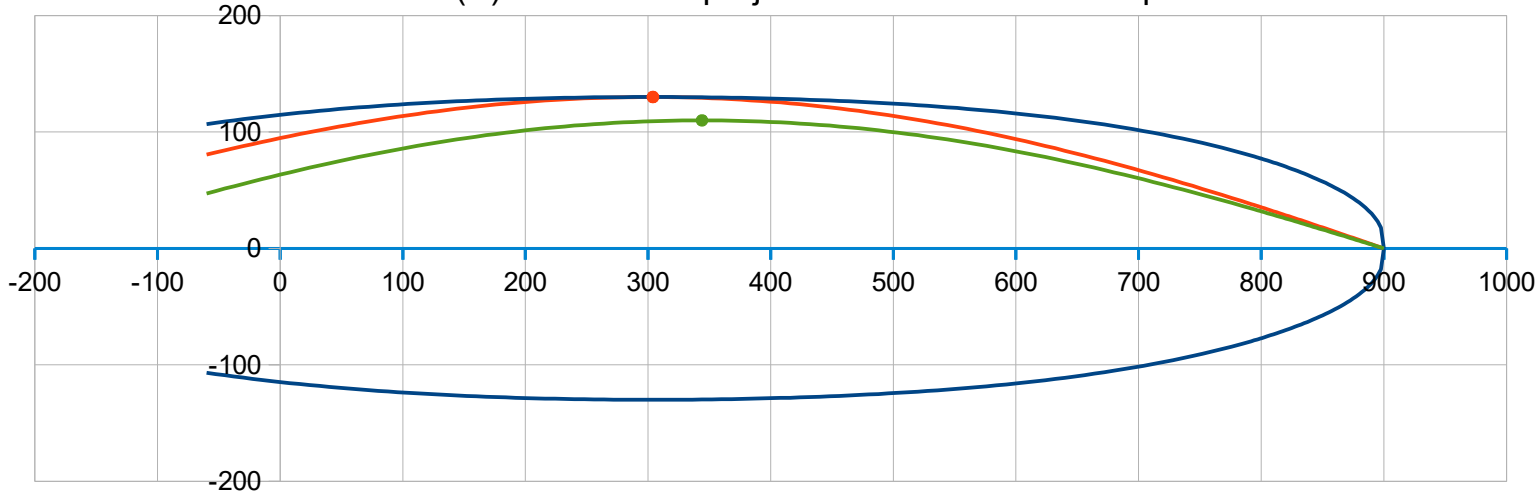
Adimensional parameters ; Scow , Pui Scow

Example , with (in addition to the above data) :

$X_{\text{tabar}} = -130,0$

$\text{Scow} = 0,80$
 $\text{Pui Scow} = 0,33$

$Y1 \text{ Alfa} + \text{Scow}(X) =$ Sheer line projection into the horizontal plan XoY

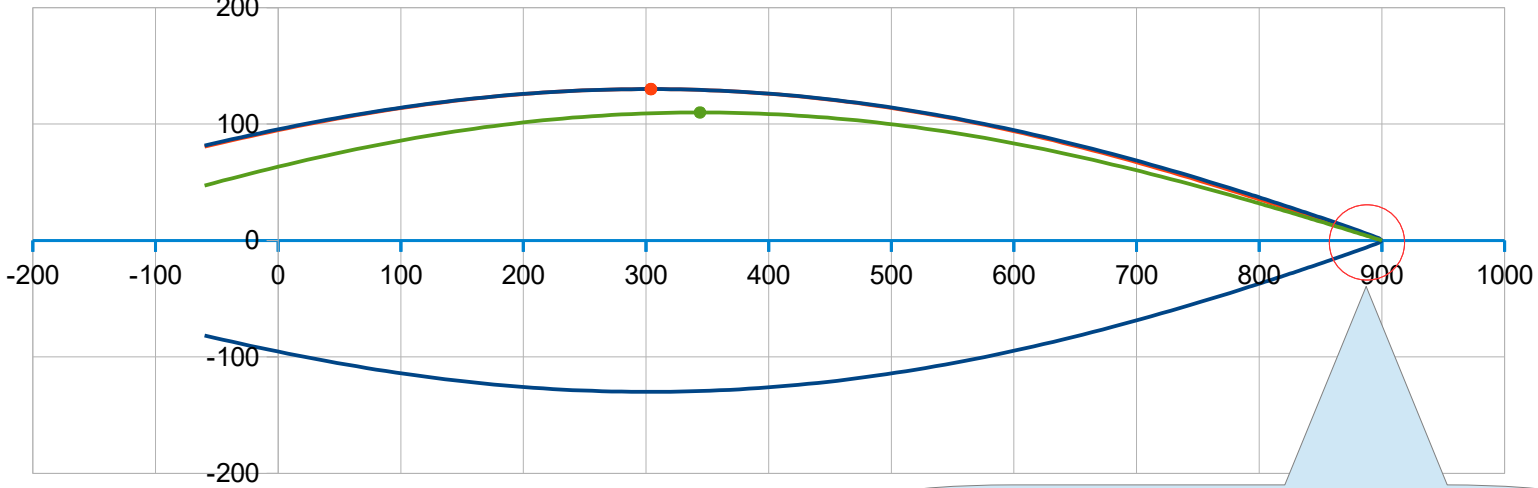


Nota : The max beam and its position is not modified by the Scow transformation

Another example : Scow parameter can be used at minima for just representing the small roundness of the bow due to the construction process, example (from boat V1) :

Scow	0,03
Pui Scow	0,25

Y1 Alfa+Scow (X) = Sheer line projection into the horizontal plan XoY

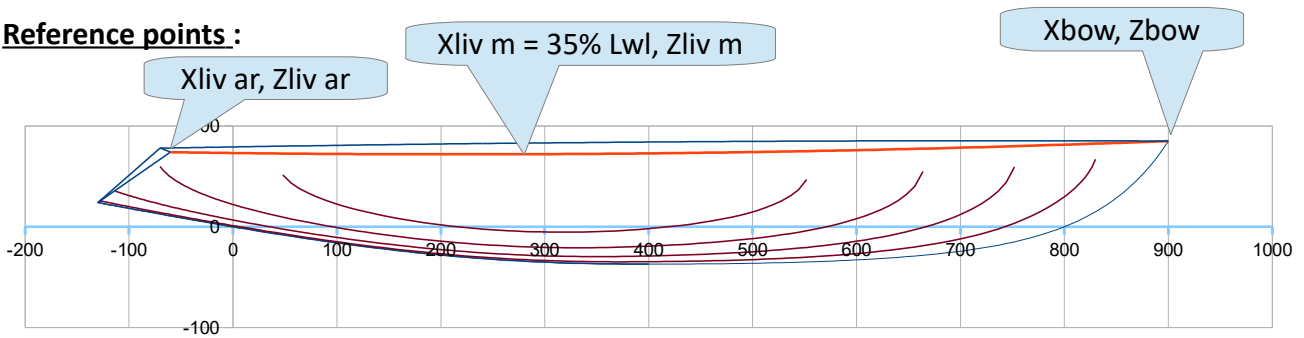


a small roundness, visible if we zoom on the bow

And also, Scow can be used while Alfa kept = 0 , the two parameters can act independently.

Sheer line / in its vertical projection xz

Reference points :



The sheer line in its vertical projection is defined by 3 reference points and a degree 2 polynome :

$$Z_1(X) = a \cdot X^2 + b \cdot X + c$$

Where

$$a = \frac{[(Z_{livm} - Z_{box}) \cdot (X_{livar} - X_{livm}) - (Z_{livar} - Z_{livm}) \cdot (X_{livm} - X_{bow})]}{[(X_{livm}^2 - X_{bow}^2) \cdot (X_{livar} - X_{livm}) - (X_{livar}^2 - X_{livm}^2) \cdot (X_{livm} - X_{bow})]}$$

$$b = \frac{[(Z_{livm} - Z_{bow}) - a \cdot (X_{livm}^2 - X_{bow}^2)]}{(X_{livm} - X_{bow})}$$

$$c = Z_{livm} - a \cdot X_{livm}^2 - b \cdot X_{livm}$$

The input data for this formulation :

Geometrical : X_{livar} , Z_{livar} , $X_{livm} = 0,35 \cdot Lwl$, Z_{livm} , X_{bow} , Z_{bow}

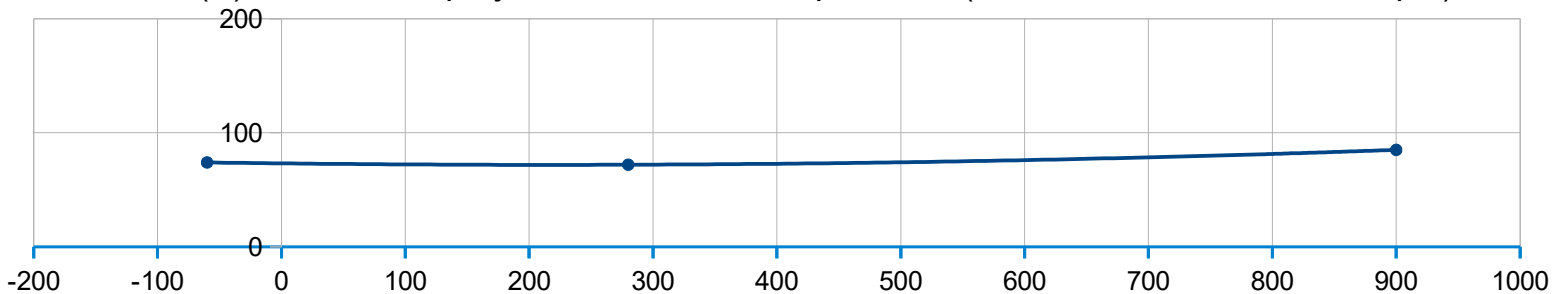
Example (from boat V1) :

X liv ar	-60,0
Z liv ar	74,0

Lwl	800,0
Sheer line at 35% Lwl	
Z liv m	72,0

Xbow	900,0
Zbow	85,0

$Z_{sheer}(X)$ = Sheer line projection in the vertical plan XoZ (based on the free-boards input)



The points show the 3 free-boards which are the input data .

In case of a vertical chine as adopted in most modern designs, the hard chine line becomes the « shear line equivalent » for the generation of the hull body under the chine .

Example from boat U1 :

