

Power required to rotate a cylinder in a moving air

Notations : for more uniformed formulations and ease further comparison,

U is the upstream flow (= the apparent wind when a sailing ship is considered)

v is the tangential speed of rotation at the surface of the rotor (>> speed ratio = v/U)

D and H are the diameter and the height of the rotor.

Sw the "wetted" surface of the rotor is then : $\pi D H$

>>> Norwood uses rotor radius a , rotor height 1,5 a and the rotational speed w, so the correspondance are :

$D = 2 a$, $H = 1,5 a$ and $v = a * w$

ρ is the air mass volumic of air (kg/m³)

Cf is the friction coefficient, computed using $Re = U * D / \nu$ and $Cf = 0,075 / (\log_{10}(Re) - 2)^2$

ν = air cinematic viscosity (m²:s)

« **Norwood** » formulation (rewritten with the above notations) :

$$P_m = C_f * (1/2 * \rho * S_w) * (2 * U^2 + v^2) * v$$

« **Norwood bis** » (when considering v for the integration in the 4th quadrant) :

$$P_m = C_f * (1/2 * \rho * S_w) * (3/2 * U^2 + 2/\pi * U * v + v^2) * v$$

>>> that presentation of the formulations highlights on the origin of the power computation (a friction force x a tangential speed of rotation) and especially on the **quadratic function of (U,v)** dimensioned as a squared speed and resulting from the integration on the cylinder perimeter.

Comparison with Reid Naca 1924 measurements :

Data of the experiments :

$D = 0,1143$ m ; $H = 1,5232$ m

$\nu = 1,429$ E-5 m²/s (estimated)

$\rho = 1,23$ kg/m³ (estimated)

Cf computed with $Re = U D / \nu$ and $Cf = 0,075 / (\log_{10}(Re) - 2)^2$ >> $Cf = 0,079$

Measurements done with $U = 15$ m/s and for 14 values of v/U from 0,4 to 1,2

Pm "Norwood" versus Pm "Reid/Naca" measurements

